

**FORWARD KINEMATICS SOLUTION FOR 5 DEGREE OF  
FREEDOM OF RHINO XR-3 ROBOT**

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**Bachelor Degree's of Mechatronic Engineering  
May 2009**

“I hereby declared that I have read through this report and found that it has comply  
the partial fulfillment for awarding the degree of Bachelor of Mechatronic  
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Date : 22 April 2009

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RHINO ROBOT**

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**This Report is Submitted in Partial Fulfillment of Requirements for the Degree  
of Bachelor in Mechatronic Engineering**

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## ABSTRACT

This project develops an algorithm for solving the forward kinematics equation. The forward kinematics equation is solving to determine the gripper position and orientation by using suitable programming software for 5 Degree of Freedom (DOF) of Rhino XR-3 robot. The process involves the control of parameter known as angles ( $\theta$ ) of rotation linkages of the three main axes of the robot. This parameter is determined by user before the forward kinematics equation is solved. Its forward kinematics problem will be solved by using conventional method and simulation. Result from the conventional method is used as guidelines for developing an algorithm to ensure the algorithm is correct and can be use for solving the forward kinematics equation. The graphical user interface will be design where user needs to setting up the value of control parameter and then solve the forward kinematics equation. The correct output of interface prove that this command can be used for solves forward kinematics equation. Overall, this project will describe the technique, calculation, method and algorithm on how the forward kinematics is solved.

## ABSTRAK

Projek ini membangunkan algoritma untuk menyelesaikan permasalahan kinematik hadapan. Permasalahan kinematik hadapan ini diselesaikan untuk menentukan kedudukan dan pergerakan cekam dengan menggunakan perisian yang sesuai untuk robot Rhino XR-3. Proses yang terlibat ialah kawalan terhadap parameter iaitu sudut putaran bagi 3 paksi. Parameter ini akan ditentukan oleh pengguna bagi menyelesaikan permasalahan kinematik hadapan tersebut. Permasalahan kinematik hadapan akan diselesaikan menggunakan kaedah konvensional dan simulasi. Hasil dari penyelesaian menerusi kaedah konvensional akan digunakan sebagai rujukan untuk membangunkan algoritma supaya algoritma tersebut sesuai dan boleh digunakan untuk menyelesaikan permasalahan kinematik hadapan. Seterusnya, pengantara muka akan dibangunkan di mana pengguna perlu memasukkan nilai parameter sebelum permasalahan tersebut diselesaikan. Hasil yang tepat dari pengantara muka ini membuktikan bahawa pengantara muka ini boleh digunakan untuk menyelesaikan permasalahan kinematik hadapan. Secara keseluruhannya, projek ini menerangkan tentang teknik, pengiraan, kaedah dan algoritma bagaimana permasalahan kinematik hadapan diselesaikan.

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## LIST OF ABBREVIATIONS

DH	-	Denavit Hartenberg
DK	-	Direct Kinematics
DOF	-	Degree of Freedom
GUI	-	Graphical User Interface
KAP	-	Kinematics Analysis Program

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## **CHAPTER 1**

### **INTRODUCTION**

The “Forward Kinematics Solution for 5 Degree of Freedom of Rhino XR-3 Robot” project is to identify and develop the programming software which is to design the graphical user interface (GUI). This GUI will be used to solve the forward kinematics problem for 5 DOF of Rhino XR-3 robot. This chapter will discuss about the background of the project, its concept, objective, scope of the project and the problem statement.

#### **1.1 BACKGROUND OF THE PROJECT**

Kinematics is the science of motion which treats motion without regard to the forces that causes it [1]. While the forward kinematics problem of Rhino XR-3 robot is to compute the position and orientation of the robot’s end-effectors relative to the base of the robot [8].

In order to solve the kinematics problem, a conventional method which has a lot of complexity equation and calculation must be applied. However, it is hard to be implemented in practice even many industrial robots are built with simple geometries to simplify the associated kinematics computations such as Rhino XR-3 robot.

It is now well accepted that the use a package of software is the best options to solve the forward kinematics problem. For this project, a graphical user interface will be designed to solve this problem which focuses only for Rhino XR-3 robot. The advantage of using this software is will minimize time for solving this problem.

## 1.2 OBJECTIVE

The main objective of this project is to solve a forward kinematics problem for 5 DOF of Rhino XR-3. In order to solve the problem, the suitable programming software will be identified and then the algorithm will be developed. After that, a user friendly GUI will be developed. Specific objectives of this project are:

- i. To identify a suitable programming software for solving forward kinematics equation.
- ii. To develop an algorithm based on the programming software.
- iii. To design a graphical user interface by using the identified of programming software and solve the forward kinematics problem for Rhino XR-3.

## 1.3 SCOPE

The scope of this project is cleared where this GUI is developed for solving the forward kinematics problem only for Rhino XR-3 robot. The GUI is also developed only for calculation the final position without any simulation of the operation of this robot. Thus, this GUI is not suitable to other type of robot unless both algorithm and GUI is modified.

Besides, the algorithm used for solve the forward kinematics is only Denavit Hartenberg (DH) Algorithm. The DH algorithm provided a systematic matrix method, based on the homogenous transformation theory to describe the position and orientation of each link of the tool tip with respect to its neighboring link in a static situation [9]. This method is chosen because it is widely used in robotics for obtaining the kinematics solutions of robot manipulators.

## 1.4 PROBLEM STATEMENT

Many industrial robots are built with simple geometries such as intersecting or parallel joint axes to simplify the associated kinematics computations. The mathematical complexity of solving robots of general architecture detracts instructors and students from using robots with arbitrary structures in illustrative examples and assignments [2].

This is also one of the major problems for the 5 Degree of Freedom of an industrial robot which is to solve the forward kinematics. Solving the forward kinematics problem need a lot of calculation when using conventional method. The complexity of formulation and computational burden make this method hard to be implemented in practice which also will waste a lot of time [10]. Therefore, a new method of solution must be developed to solve the forward kinematics equation such as using programming software.



## **CHAPTER 2**

### **LITERATURE REVIEW**

In this chapter, a review of previous research project that are related with this project will be discussed. The information about forward kinematics and Rhino XR-3 robot are also described in this chapter.

#### **2.1 DK ANALYSIS OF 5 AXIS RHINO XR-3 ROBOT**

DK Analysis of 5 Axis Rhino XR-3 Robot is C++ programs written without GUI by N.R. Narayana Murthy [3] for solving the forward kinematics for Rhino XR-3 robot. However, this program still useful for research where the output of the program is used as a comparison with the program of this project.

This program allowed user to enter the Denavit Hartenberg (DH) parameter table for the robot to perform the forward kinematics. The DH-parameters can be entered from the keyboard. Then, the calculation for the transformation matrix of base frame with respect to next frame is done one by one for 5 degree of freedom. Finally, the final position of the gripper for Rhino XR-3 robot is obtained.

The program and output for direct kinematics analysis of 5 axis Rhino XR-3 robot is as Appendix 2. Some editing should be done to this program since some error occurs when running the program.

## 2.2 Sirf Rhino (RhinoGui Interface)

The RhinoGui is an interface developed by Venkatraghavan Gourishankar, (May 2006) which can be used to experiment with the basic kinematics of the Rhino XR-3 robot [4]. The user interaction with the interface has been made as simple as possible. Three main files, the „RhinoForwardKinematics.m“, „RhinoInverse.m“ and „trajectory.m“ work behind the interface in providing the user with the kinematics of the robot. The „Robotics toolbox for Matlab“ is installed provides the visualization automatically [4].

The RhinoGui interface is shown in Figure 2.1. The forward Kinematics can be performed on the robot by setting up the required joint angles either by the edit box or by the sliders and then clicking the button named „Forward Kinematics“. As soon as the forward kinematics button is clicked, the plot of the robot configuration changes to the user set configuration. The Arm matrix for the current configuration is also updated accordingly. The startup values for the joint angles and the arm matrix are the values for the Rhino XR-3 robot in its home position. The home position has the following joint angles and arm matrix Joint angles –  $\theta_1 = 0$ ,  $\theta_2 = -90$ ,  $\theta_3 = 90$ ,  $\theta_4 = 0$  and  $\theta_5 = 0$ . All the joint angles are in degrees. All values are in meters. By default the last row of the arm matrix is not shown in the interface since it remains the same all the time [4].

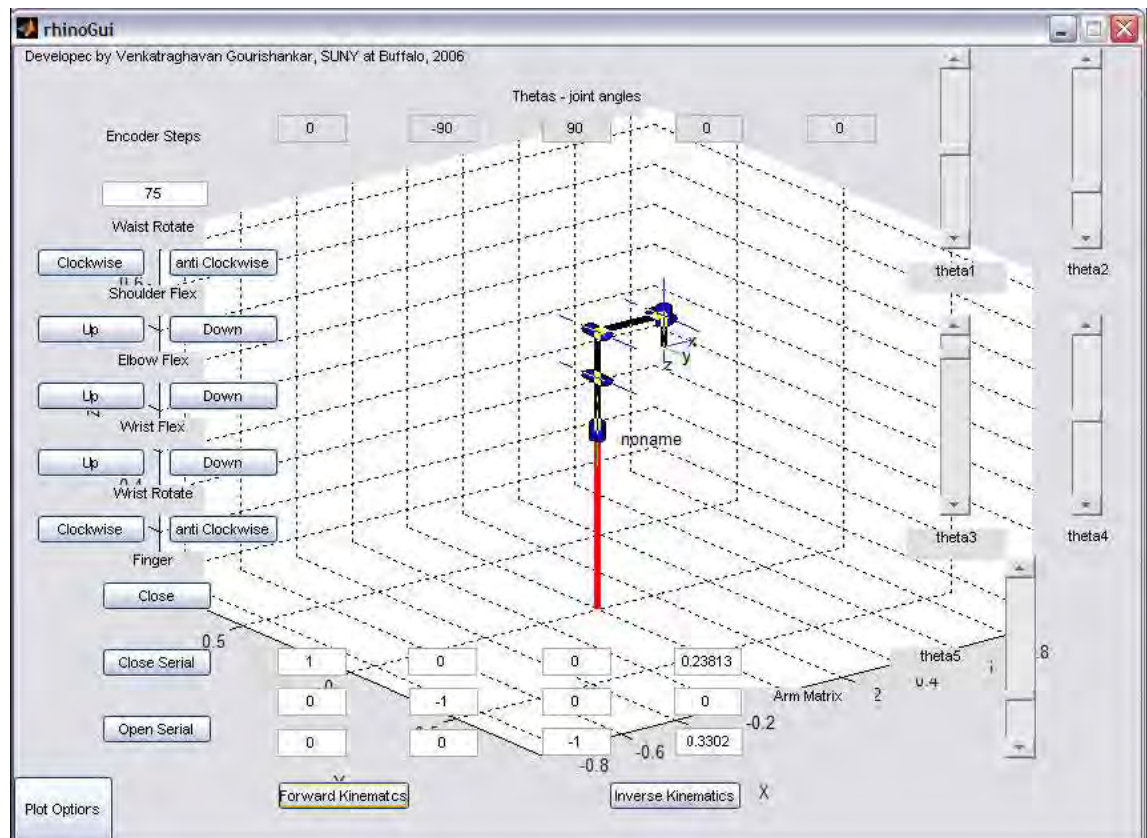


Figure 2.1: RhinoGui interface.

### 2.3 Kinematics Analysis Program (KAP)

Kinematics Analysis Program is a program developed by Rachid Manseur [2]. KAP is currently developed to compute the forward and inverse kinematics of robot manipulators with 5 or 6 revolute degrees of freedom. The functional block diagram of KAP is shown on Figure 2.3. There are two type of KAP:

- i. KAP5 – to compute the inverse kinematics problem for 5 DOF of Rhino XR-3 robot (See Figure 2.2).
- ii. KAP6 – to compute the forward kinematics of Fanuc robot.

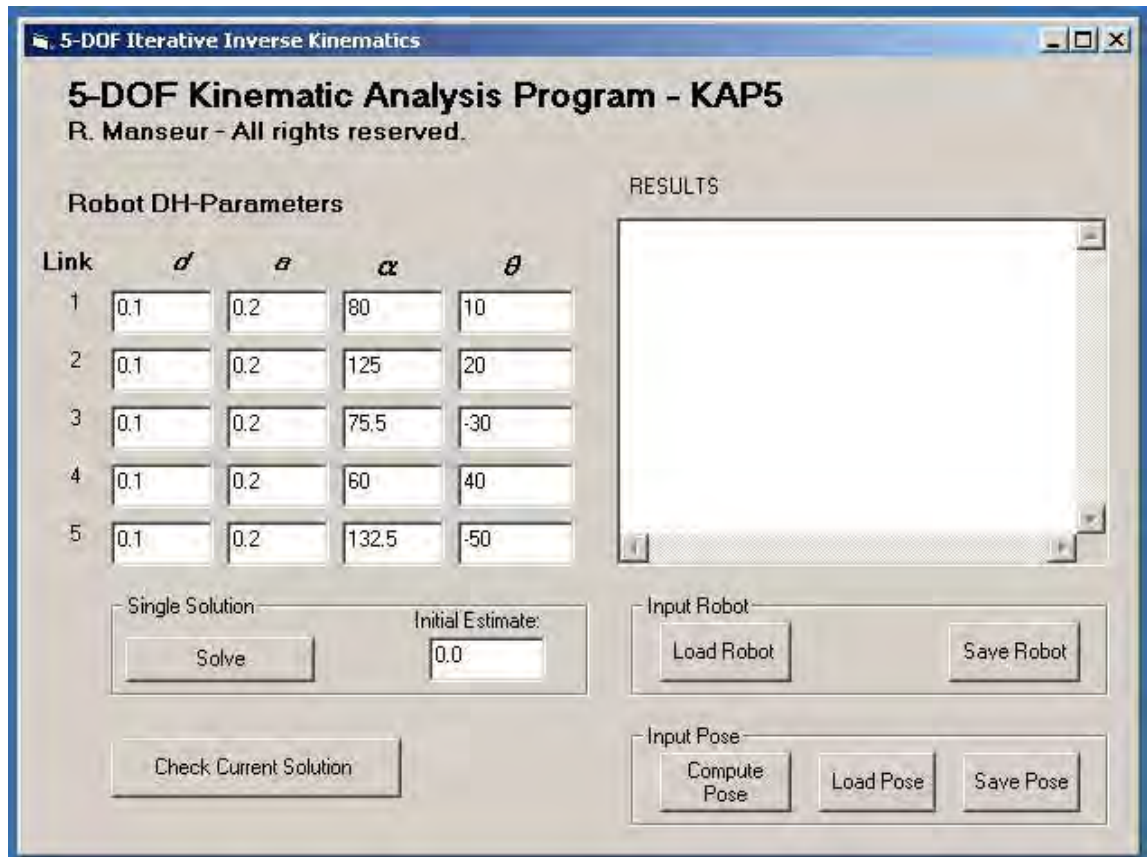


Figure 2.2: GUI of KAP5.

In this program, the user is asked to enter the DH parameters table for the robot. The DH parameters can be entered from the keyboard or by specifying a pre-existing file name containing the robot DH parameters in the format shown on Table 2.1. The end effectors pose can also be entered through the keyboard, read from a pre-existing file named POSE.DAT, or computed from joint angles that the user enters through the forward kinematics block. The program determines the number of DOFs of the robot and applies the proper algorithm [2]. Even this program is to compute the inverse kinematics of Rhino XR-3 robot, it still useful as a sample for design a GUI for this project.

Table 2.1: Robot DH-parameter table

Link	$d$	$a$	$\alpha$	$\theta$
1	$d_1$	$a_1$	$\alpha_1$	$\theta_1$
2	$d_2$	$a_2$	$\alpha_2$	$\theta_2$
3	$d_3$	$a_3$	$\alpha_3$	$\theta_3$
4	$d_4$	$a_4$	$\alpha_4$	$\theta_4$
5	$d_5$	$a_5$	$\alpha_5$	$\theta_5$

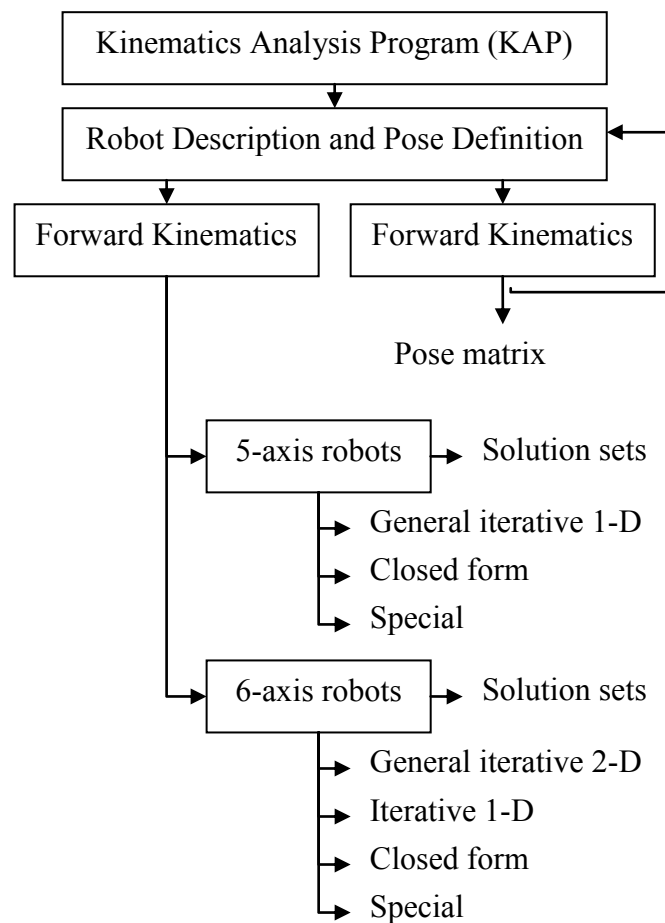


Figure 2.3: Functional Block Diagram of KAP

## 2.4 Forward Kinematics

The forward kinematics problem is concerned with the relationship between the individual joints of the robot manipulator and the position and orientation of the tool or end-effector. Stated more formally, the forward kinematics problem is to determine the position and orientation of the end-effector, given the values for the joint variables of the robot [5].

In order to describe the location of each link relative to its neighbors we define a frame attached to each link. The link frames are named by number according to the link to which they are attached. That is, frame  $\{i\}$  is attached rigidly to link  $i$ . To locate frames on the links, this convention is used: The Z-axis of frame  $\{i\}$ , called  $Z_i$  is coincident with the joint axis  $i$ . The origin of frame  $\{i\}$  is located where  $a_i$  perpendicular intersects the joint  $i$  axis.  $X_i$  points along  $a_i$  in the direction from joint  $i$  to joint  $i+1$  [1].

In the usual case of revolute joint,  $\theta_i$  is called the joint variable, and the other three quantities would be fixed link parameters. For prismatic joints,  $d_i$  is the joint variable and the other three quantities are fixed link parameters. The definition of mechanism by means of these quantities is a convention usually called DH notation [1].

### 2.4.1 Denavit Hartenberg Representation

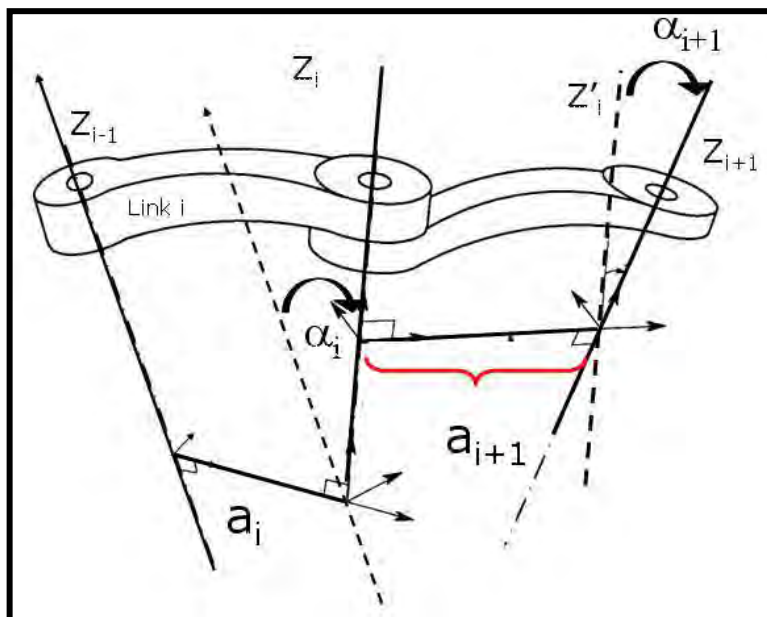


Figure 2.4: Link Parameter.

A commonly used convention for selecting frames of reference in robotic applications is the Denavit-Hartenberg, or DH convention. In this convention, each homogeneous transformation  $A_i$  is represented as a product of four basic transformations. The procedure based on the DH convention in the following algorithm for deriving the forward kinematics for any manipulator are summarize as below [5]:

Step 1 : Locate and label the joint axes  $z_0, \dots, z_{n-1}$ .

Step 2 : Establish the base frame. Set the origin anywhere on the  $z_0$ -axis. The  $x_0$  and  $y_0$  axes are chosen conveniently to form a right-hand frame. For  $i = 1, \dots, n-1$ , perform Steps 3 to 5.

Step 3 : Locate the origin  $O_i$  where the common normal to  $z_i$  and  $z_{i-1}$  intersects  $z_i$ . If  $z_i$  intersects  $z_{i-1}$  locate  $O_i$  at this intersection. If  $z_i$  and  $z_{i-1}$  are parallel, locate  $O_i$  in any convenient position along  $z_i$ .

Step 4: Establish  $x_i$  along the common normal between  $z_{i-1}$  and  $z_i$  through  $O_i$ , or in the direction normal to the  $z_{i-1} - z_i$  plane if  $z_{i-1}$  and  $z_i$  intersect.

Step 5 : Establish  $y_i$  to complete a right-hand frame.

Step 6 : Establish the end-effector frame  $o_n x_n y_n z_n$ . Assuming the  $n^{\text{th}}$  joint is revolute set  $z_n = a$  along the direction  $z_{n-1}$ . Establish the origin  $o_n$  conveniently along  $z_n$ , preferably at the center of the gripper or at the tip of any tool that the manipulator may be carrying. Set  $y_n = s$  in the direction of the gripper closure and set  $x_n = n$  as  $s \times a$ . If the tool is not a simple gripper set  $x_n$  and  $y_n$  conveniently to form a right-hand frame.

Step 7 : Create a table of link parameters  $a_i, d_i, \alpha_i, \theta_i$ .

$a_i$  = Distance along  $x_i$  from  $o_i$  to the intersection of the  $x_i$  and  $z_{i-1}$  axes.

$d_i$  = Distance along  $z_{i-1}$  from  $O_{i-1}$  to the intersection of the  $x_i$  and  $z_{i-1}$  axes.

$d_i$  is variable if joint  $i$  is prismatic.

$\alpha_i$  = The angle between  $z_{i-1}$  and  $z_i$  measured about  $x_i$  (see Figure 2.4).

$\theta_i$  = The angle between  $x_{i-1}$  and  $x_i$  measured about  $z_{i-1}$  (see Figure 2.4).  $\theta_i$  is variable if joint  $i$  is revolute.

Step 8 : Form the homogeneous transformation matrices  $A_i$  by substituting the above parameters into equation 2.1.

Step 9 : Form  $T_n^0 = A_1 \dots A_n$ . This then gives the position and orientation of the tool frame expressed in base coordinates.

The overall transformation is obtained by post multiplication of individual transformations:

$$T_i^{i+1} = Rot(z, \theta_i) Trans(0, 0, d_i) Trans(0, 0, a_i) Rot(x, \alpha_i) \quad (2.1)$$

$$T_i^{i+1} = \begin{bmatrix} c\theta_i & -s\theta_i & 0 & 0 \\ s\theta_i & c\theta_i & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & a_i \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & c\alpha_i & -s\alpha_i & 0 \\ 0 & -s\alpha_i & c\alpha_i & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (2.2)$$