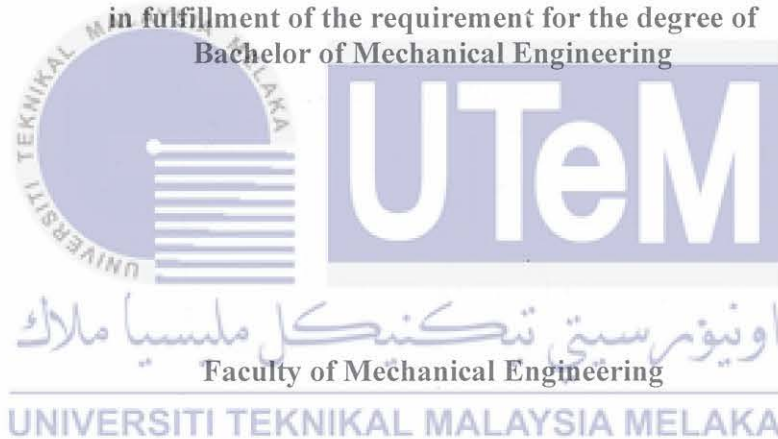


**PATH TRACKING FOR UNINTENDED ROADWAY DEPARTURE**

**KELVIN LOI HUI KOK**

**This report is submitted  
in fulfillment of the requirement for the degree of  
Bachelor of Mechanical Engineering**



**UNIVERSITI TEKNIKAL MALAYSIA MELAKA**

**AUGUST 2021**

## DECLARATION

I declare that this project report entitled “Path Tracking for Unintended Roadway Departure”  
is the result of my work except as cited in the references

Signature : Li  
Name : Kelvin Loi Hui Kok  
Date : 14/9/21



اونيورسيتي تيكنيكل مليسيا ملاك

UNIVERSITI TEKNIKAL MALAYSIA MELAKA

## APPROVAL

I hereby declare that I have read this project report and in my opinion, this report is sufficient in terms of scope and quality for the award of the degree of Bachelor of Mechanical Engineering.

Signature :   
Name of Supervisor : Dr. Amrik Singh<sup>9/11</sup> Phuman Singh  
Date : 17/09/2021



اونيورسيتي تيكنيكل مليسيا ملاك  
UNIVERSITI TEKNIKAL MALAYSIA MELAKA

## DEDICATION

To my beloved mother and father



## ABSTRACT

Unintended roadway departure (URD) has been one of the main causes of traffic fatalities. New technologies such as autonomous steering that automatically detect departure from the lane and provide interventions could help prevent unintended roadway departure. This study is aimed at developing and evaluating the effectiveness of a path tracking controller for unintended road departure. To achieve this, a path tracking controller is designed which comprises feedforward, feedback, and yaw controllers. A 2-DOF vehicle model with a Brush tire model is implemented as the control system plant. The lane-keeping controller is built and simulated using MATLAB Simulink. From the result, the cornering force increases with increasing friction coefficient due to the increased contact stresses because of tire deformation. The controller's performance is evaluated using various velocities. The result shows that the controllers can track the desired path with relatively small lateral error with an increasing velocity. As velocity increases, the maximum absolute tire force usage increases due to the higher centrifugal force. Maximum absolute lateral error, heading error, and yaw rate error also increases with increasing velocity. We can conclude that as velocity increase, the ability for the controller to track the path decrease.

## ABSTRAK

Permegian jalan raya yang tidak disengajakan merupakan salah satu penyebab utama kemalangan jalan raya. Teknologi baru seperti stereng autonomi yang dapat mengesan keberangkatan dari lorong secara automatik serta memberikan campur tangan dapat membantu mencegah keberangkatan jalan raya yang tidak diingini. Tujuan kajian ini adalah untuk membina dan menilai keberkesanan pengawal penjejakan laluan untuk keberangkatan jalan yang tidak disengajakan. Untuk mencapai tujuan ini, pengawal penjejakan laluan yang terdiri daripada feedforward, maklum balas, dan menguap telah dirancangkan. Model kenderaan 2-DOF dengan model tayar Brush diimplementasikan sebagai loji untuk system kawalan. Pengawal penjejakan laluan dibina dan disimulasikan menggunakan MATLAB Simulink. Dari hasil keputusan, daya penjuru meningkat dengan peningkatan pekali geseran disebabkan oleh peningkatan tegangan senthuan menegak dan melintang akibat ubah bentuk tayar. Halaju yang berbeza telah digunakan untuk menilai prestasi pengawal. Hasilnya menunjukkan bahawa pengawal dapat mengesan jalan yang diinginkan dengan kesilapan lateral yang agak kecil dengan halaju yang semakin meningkat. Penggunaan daya tayar mutlak maksimum meningkat dengan halaju kerana daya sentrifugal yang lebih tinggi. Apabila halaju meningkat, kesilapan lateral mutlak maksimum, ralat arah, dan ralat kadar menguap juga meningkat. Kita dapat menyimpulkan bahawa apabila halaju meningkat, kemampuan pengawal untuk mengesan jalan menurun.

## ACKNOWLEDGEMENT

I would like to give thanks to Dr. Amrik Singh, my supervisor, for guiding me through the final year project. His enthusiasm, patience, and advice have helped me tremendously in my final year of study. He always provides guidance and expertise whenever I face any issues regarding the project. He always finds time to conduct weekly meetings to make sure that our works are progressing smoothly despite his busy schedule.

Secondly, I'd like to express my gratitude to University Teknikal Malaysia Melaka for accepting me into the graduate program. I'd also like to show my appreciation to the Faculty of Mechanical Engineering for teaching me knowledge of engineering.

UNIVERSITI TEKNIKAL MALAYSIA MELAKA

I'd like to thank my friends for their encouragement, patience, and support. Lastly, I'd want to thank my family for their unwavering support.

## CONTENT

CHAPTER	CONTENT	PAGE
	SUPERVISOR'S DECLARATION	i
	TABLE OF CONTENT	vii
	LIST OF FIGURES	xi
	LIST OF TABLES	xiii
	LIST OF ABBREVIATIONS	xiv
	LIST OF SYMBOLS	xvi
CHAPTER 1	INTRODUCTION	1
	1.1 Motivation	1
	1.2 Background	3
	1.3 Objectives	4
	1.4 Scope of Project	5
	1.5 General Methodology	5



<b>CHAPTER 2</b>	<b>LITERATURE REVIEW</b>	7
2.1	Collision Avoidance Scenarios	7
2.2	Vehicle Dynamics Model	10
2.2.1	Two-Degree-of-Freedom Vehicle Model	10
2.2.2	Three-Degree-of-Freedom Vehicle Model	12
2.2.3	Seven-Degree-of-Freedom Vehicle Model	13
2.2.4	Fourteen-Degree-of-Freedom Vehicle Model	16
2.3	Tire Model	17
2.3.1	Magic Tire Model	17
2.3.2	Dugoff Tire Model	18
2.3.3	Brush Tire Model	19
2.4	Trajectory Tracking Control	20
2.4.1	Model Predictive Control	20
2.4.2	PID Control	21
2.4.3	Linear Quadratic Control	22
2.4.4	Direct Yaw Moment Control	22
2.4.5	Sliding Mode Control	23
2.5	MATLAB and Simulink	24



<b>CHAPTER 3</b>	<b>METHODOLOGY</b>	25
3.1	Introduction	25
3.2	Vehicle Dynamic Model	27
3.3	Brush Tire Model	28
3.4	Unintended Roadway Departure Scenario	29
3.5	Design of a Path Tracking Controller	30
3.5.1	Feedforward Control	31
3.5.2	Feedback Control	33
3.5.3	Yaw Control	34
<b>CHAPTER 4</b>	<b>RESULT AND DISCUSSION</b>	37
4.1	Simulation Result of Brush Tire Model	37
4.2	Path Tracking at Different Velocity	38
4.3	Tire Force Usage	39
4.4	Maximum Absolute Lateral Error	40
4.5	Maximum Absolute Heading Error	41
4.6	Maximum Absolute Yaw Rate Error	42



<b>CHAPTER 5</b>	<b>CONCLUSION AND RECOMMENDATIONS</b>	44
5.1	Conclusion	44
5.2	Recommendations	44
	<b>REFERENCE</b>	46



## LIST OF FIGURES

FIGURE	TITLE	PAGE
1.1	Malaysia's total road and motor vehicle accidents from 2007-2016	2
2.1	A phased highway maneuver consisting of (a) "Pure obstacle avoidance" maneuver, (b) "Barrier avoidance" maneuver, and (c) "Recovery" maneuver (Dingle, 2010)	8
2.2	Overtaking maneuver with oncoming traffic (Levulis et al, 2015)	9
2.3	Unintended roadway departure (Alleyne, 1997)	10
2.4	2-DOF vehicle model (Ono et al., 1998)	11
2.5	3-DOF vehicle model (Falcone, 2007)	12
2.6	7-DOF vehicle model (Khaknejad, 2012)	14
2.7	Free-body diagram of a wheel (Khaknejad, 2012)	14
2.8	14-DOF vehicle model (Liu, 2013)	16
3.1	Methodology flow chart for PSM I	26
3.2	Methodology flow chart for PSM II	27
3.3	2-DOF bicycle model	28

3.4	Unintended roadway departure problem description	30
3.5	Block diagram of the lane-keeping control system	31
3.6	Definition of heading error ( $\Delta\psi$ ) and lookahead error ( $e_{la}$ )	33
4.1	Cornering force, $F$ against slip angle, $\alpha$ with friction coefficient of (a) $\mu = 0.2$ , (b) $\mu = 0.5$ , and (c) $\mu = 0.9$	38
4.2	Path tracking at (a) $v_x = 20$ m/s, (b) $v_x = 25$ m/s, (c) $v_x = 30$ m/s and (d) $v_x = 35$ m/s	39
4.3	Peak tire force usage at different velocities	40
4.4	Maximum absolute lateral error at different velocities	41
4.5	Maximum absolute heading error at different velocities	42
4.6	Maximum absolute yaw rate error at different velocities	43



## LIST OF TABLES

TABLE	TITLE	PAGE
4.1	Maximum absolute tire force usage at different velocities	40
4.2	Maximum absolute lateral error at different velocities	41
4.3	Maximum absolute heading error	42
4.4	Maximum absolute yaw rate error	43



## LIST OF ABBREVIATIONS

ARE Algebraic Ricatti Equation

DYC Direct Yaw-Moment Control

LDW Lane Departure Warning Systems

LKA Lane Keeping Assist

LQG Linear Quadratic Gaussian

LQR Linear Quadratic Regulator

MPC Model Predictive Control

NHTSA National Highway Traffic Safety Administration

PID Proportional, Integral, and Derivative

SMC Sliding Mode Control

URD Unintended Roadway Departure

2-DOF 2 Degree of Freedom

3-DOF 3 Degree of Freedom

7-DOF 7 Degree of Freedom



14-DOF      14 Degree of Freedom

2WS          Two Wheel Steering

4WS          Four Wheel Steering





## LIST OF SYMBOLS

$a_y$	-	Vehicle's lateral acceleration
$c$	-	Lateral axle cornering stiffness
$c_\alpha$	-	Tire cornering stiffness
$c_f$	-	Cornering stiffness of front axle
$c_r$	-	Cornering stiffness of rear axle
$e$	-	Distance between desired path and center of gravity
$e_{la}$	-	Lookahead error
$f_r$	-	Rolling resistance coefficient
$F_{xi}$	-	Longitudinal tire force
$F_{yf}$	-	Front lateral tire force
$F_{yi}$	-	Lateral tire force
$F_{yr}$	-	Rear lateral tire force
$F_{zf}$	-	Front axle normal load

$F_{zr}$	-	Rear axle normal load
$g$	-	Gravitational acceleration
$J_i$	-	Wheel moment of inertia
$J_z$	-	Yaw moment of Inertia
$k_p$	-	Lanekeeping potential field gain
$K_{US}$	-	Understeer gradient
$k_{\Delta\psi}$	-	Yaw damping gain
$l$	-	Length of the vehicle
$l_f$	-	Distance between center of gravity and front axle
$l_r$	-	Distance between center of gravity and rear axle
$m$	-	Mass of the vehicle
$R_w$	-	Wheel's effective radius
$T_{bi}$	-	Wheel braking torque
$T_f$	-	Front track
$T_i$	-	Wheel traction torque
$T_{Roll}$	-	Rolling resistance torque
$v$	-	Velocity
$v_x$	-	Longitudinal velocity

$v_y$	-	Lateral velocity
$x_{la}$	-	Lookahead distance
$\alpha_f$	-	Slip angle of the front tire
$\alpha_r$	-	Slip angle of the rear tire
$\beta$	-	Vehicle sideslip angle
$\gamma$	-	Yaw rate
$\delta$	-	Steering angle
$\delta_{control}$	-	Feedback steering angle
$\delta_f$	-	Front steering angle
$\delta_{ff}$	-	Feedforward steering angle
$\delta_{yaw}$	-	Yaw control steering angle
$\kappa$	-	Path curvature
$\mu$	-	Surface coefficient of friction
$\Delta\psi$	-	Heading error
$\psi_{CG}$	-	Vehicle's heading angle relative to the earth frame
$\psi_r$	-	Path's heading angle relative to the earth frame

## CHAPTER 1

### INTRODUCTION

#### 1.1 Motivation

Traffic accidents and related deaths have been increasing in Malaysia due to the growing population and vehicles on the roads. The number of accidents had increased from 148,801 accidents to 326,817 accidents as the population of Malaysia grows from 19,494,000 in 1994 to 25,600,000 in 2004 (Umar, 2005). This unnerving situation needs to be restrained to save lives and reduce economic loss. According to data from the Malaysian Ministry of Transport, the overall number of road accidents grew by 41% from 2007 to 2016, from 369,319 to 521,466. (Ministry of Transport, 2016). The total number of deaths was increased from 6282 to 7152. The total number of vehicles involved in road accidents rises by almost 44%, from 666,027 to 960,569 in the same period. Figure 1.1 shows Malaysia's total road and motor vehicle accidents from 2007-2016 (Ministry of Transport, 2016).

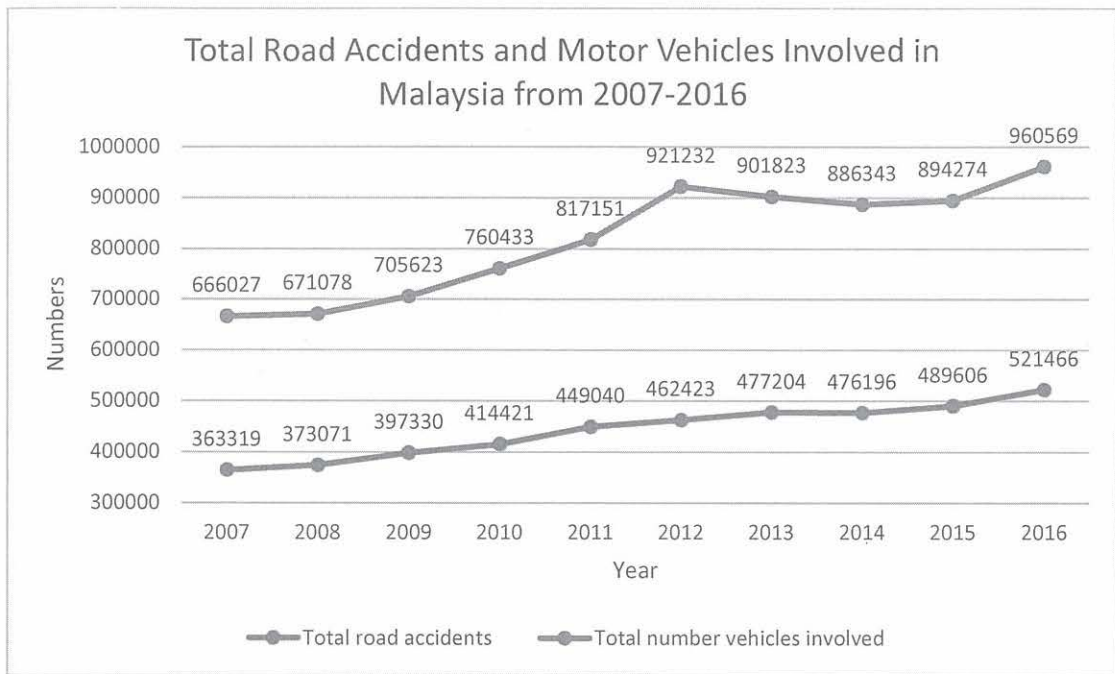


Figure 1.1: Malaysia's total road and motor vehicle accidents from 2007-2016 (Ministry of Transport, 2016)

Road safety monitoring remains inadequate in contempt with the extensive financing of the Malaysian Government. Road safety aspects are detrimentally impacted by the escalating mobility of modern society. Dangerous turning, speeding, and other offenses are the most reported causes of accidents in Malaysia, which occupy 28.8%, 16.1%, and 15.8%, respectively. (Abdelfatah, 2016).

One of the main causes of traffic fatalities is Unintended Roadway Departures (URD). (Alleyne, 1997). A URD happens when the vehicle swerves away from its intended path without the driver's control (Alleyne, 1997). Unintended Roadway Departure (URD) is often caused by distraction, fatigue, and other acts of negligence and failure to command the path of the vehicle track to coincide with the road direction. Human error is responsible for 94% to 96% of vehicle crashes as stated by the 2016 fatality report (Bruce, 2017).

Implementation of intelligent road systems makes roads safer and minimizes the accidents occurring. New technologies such as autonomous steering that automatically detect departure from the lane and provide interventions could help prevent unintended roadway departure as driver error is eliminated from the equation.

## 1.2 Background

An autonomous vehicle is a vehicle that operates itself by sensing its environment and operating without human intervention. Autonomous automotive systems are growing at a remarkable pace. Self-driving technologies are developed by major automakers such as Tesla, Uber, Google, and Nissan. Autonomous vehicles map and interpret their surroundings by using a wide array of sensors. The software then processes the information and commands vehicle's the 'actuator' to make an intervention, which can be steering, braking, and acceleration. These autonomous technologies could assist the driver during emergencies to prevent unintended roadway departure.

Lane departure systems like the Lane Departure Warner System (LDW) detect and alert the driver when the vehicle leaves its intended path with sound, visual, or vibration alerts. However, an appropriate response is required from the driver, which they may be unable to perform. The response of these systems if the driver does not take control after the system has intervened determines whether or not they can avert a crash. That said, a driverless lane-keeping assist needs to take over during emergencies to prevent crashes. Several automakers have built their LKA (Lane Keeping Assist) systems in many variants to improve lane assist and decrease the number of accidents caused by unintended roadway departures (Kang, 2017). Lane Keeping Assist (LKA) is a technology that warns the driver if the vehicle is straying out of its lane. and, with no response, automatically make interventions to correct

the vehicle's path. These systems improve lane control via torque created on the steering wheel or controlling of rotation of the steering wheel is turned. These systems are able to maintain lane-keeping by controlling the steering wheel angle or through torque generation on the steering wheel (Hwang, 2008).

This study is aimed at developing and evaluating the effectiveness of a path tracking controller for unintended road departure. To achieve this, a path tracking controller is designed which comprises feedforward, feedback, and yaw controllers. The control system uses a 2-DOF vehicle handling model as its plant. To assure the vehicle's tracking ability, various vehicle feedback states are used. This control is proposed so that under all conditions, the vehicle is able to maintain its stability and maneuverability (Ono et. al., 1998). Most modern vehicles steer by only turning the front wheels. This means that the driver uses only one input, the front steering angle, to regulate the vehicle's lateral acceleration and yaw rate.

Different techniques, such as linear quadratic Gaussian (LQG), sliding mode, adaptive, and nonlinear control were used for designing vehicle control systems. To design the path tracking control system, MATLAB Simulink is used. The control system performance is assessed by utilizing a 2-DOF vehicle handling model.

### 1.3 Objectives

The objectives of this project are as following:

1. To develop a path tracking controller for unintended road departure.
2. To evaluate the effectiveness of the path tracking controller.

## 1.4 Scope

The scope of this project includes the following:

1. Development of the nonlinear vehicle handling model.
2. Design of the path tracking control system in Simulink.
3. Performance evaluation of the path tracking controller.

## 1.5 General Methodology

In this project, the following are the steps required to establish the objectives :

1. Literature review

Journal, articles, websites, or other sources related to the topic of the project will be reviewed to understand the fundamental of the topic.

2. Derivation of the vehicle dynamics model

The mathematical model of each segment will be developed for path tracking by using a 2-DOF bicycle model with a Brush tire model and the equations of motion of the bicycle model will be derived.

3. Design of a path tracking controller

Path tracking controller operates by using an autonomous steering input. The steering controller comprises feedforward, feedback, and yaw components. A bicycle model is used to predict the steering input to track the path. A lane-keeping steering feedback system is used to reduce errors induced by disturbances or modeling errors. A yaw control system is used to minimize yaw errors.

4. Building MATLAB Simulink diagram for path tracking control system.

The vehicle dynamics model and control system are constructed by using MATLAB SIMULINK.